

A NEW FORM OF b-OPEN SETS IN INFRA TOPOLOGICAL SPACE

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Abstract:The purpose of this paper is to introduce a new class of infra open sets in infra topological spaces called infra b-open sets. The relationships among infra b-open sets and other open sets in infra topological settings are discussed. This paper also throws light on the various forms of continuity via infra topological space and explores its properties.

Keywords:Infra b-Open Sets, Infra b-Continuous Functions Infra b- Irresolute Functions.

1. Introduction: In 1996, D.Andrijevic'[3] introduced and studied the class of generalized open sets in a topological space called b-open sets .This class of sets is contained in the β -open sets [4], which contains all semi-open sets [5], and all pre-open sets[7]. Adel.M.AL.Odhari [1,2] introduced the concept of infra topological space and studied infra continuous and infra continuous functions. O.Njastad[8] introduced some classes of nearly open sets. Vidyottamakumari, Thakur C.K. Raman [9] proposed the various characterizations of b-open sets in a topological space.

2. Preliminaries: Definition 2.1: Let X be any arbitrary set. An Infra -topological space on X is a collection τ_{iX} subsets of X such that the following axioms are satisfying:

Ax-1: $\phi, X \in \tau_{iX}$.

Ax-2: The intersection of the elements of any sub collection of τ_{iX} in X.

i.e) If $O_i \in \tau_{iX}, 1 \leq i \leq n \rightarrow \cap O_i \in \tau_{iX}$.

Terminology, the order pair (X, τ_{iX}) is called infra-topological space. We simply say X is an infra space.

Definition 2.2: Let (X, τ_{iX}) be an infra-topological space and $A \subset X$. A is called infra open set (IOS) if $A \in \tau_{iX}$

Definition 2.3: Let (X, τ_{iX}) be an infra topological space. A subset $C \subset X$ is called infra-closed set (ICS) in X if $X \setminus C$ is infra-open set in X.(i.e) C is infra-closed set (ICS) iff $X \setminus C \in \tau_{iX}$.

Definition 2.4: Let (X, τ_{iX}) be an infra topological space and $A \subset X$. The **Infra Closure Point (ICP)** of A is a set denoted by $icp(A)$ and given by :

$$icp(A) = \cap \{C_i : A \subseteq C_i, X - C_i \in \tau_{iX}\}$$

(i.e) $icp(A)$ is the intersection of all infra closed set containing the set A.

Definition 2.5: Let (X, τ_{iX}) be an infra topological space and $A \subset X$. The **Infra Interior Point (IIP)** of A is a set denoted by $iip(A)$ and given by:

$$iip(A) = \cup \{O_i : O_i \subseteq A, O_i \in \tau_{iX}\}$$

(i.e) $iip(A)$ is the union of all infra open set contained in the set A.

Definition 2.6: Let (X, τ_X) be a topological space and Let (X, τ_{iX}) be an infra topological space. We say that τ_{iX} is an infra-topological space associated with τ_X , if $\tau_{iX} \subset \tau_X$.

Definition 2.7: Let (X, τ_X) and (Y, τ_Y) be represent two topological spaces and τ_{iX} be associated infra topological space with τ_X . A function $f: X \rightarrow Y$ is called I- continuous function at $x \in X$, if \forall open set O containing $f(x)$ in Y, then \exists Infra open set U containing x in τ_{iX} such that $f(U) \subset O$.

Definition 2.8: Let (X, τ_X) and (Y, τ_Y) be represent two topological spaces. Let τ_{iX} and τ_{iY} be associated infra topological space with τ_X and τ_Y respectively. A function $f: X \rightarrow Y$ is called I - continuous function, if the inverse image of each infra open set in τ_{iY} is an τ_{iX} infra open set in X.

3. Infra B-Open Sets In Infra Topological Space:

In this section, we introduce the concept of new infra open sets such as infra semi- open set, infra pre- open set, infra α -open set, infra b-open set, infra semi-preopen set (or) infra β -open in an infra topological space and study some of its properties.

Definition 3.1: Let (X, τ_{iX}) be an infra topological space. A set 'A' is called infra semi-open if $A \subseteq icp(iip(A))$ and infra semi- closed set if $icp(iip(A)) \subseteq A$.

Definition 3.2: Let (X, τ_{iX}) be an infra topological space. A set 'A' is called infra pre-open if $A \subseteq iip(icp(A))$ and infra pre- closed set if $iip(icp(A)) \subseteq A$.

Definition 3.3: Let (X, τ_{iX}) be an infra topological space. A set 'A' is called infra α -open if $A \subseteq iip(icp(iip(A)))$ and infra α - closed set if $iip(icp(iip(A))) \subseteq A$.

Definition 3.4: Let (X, τ_{iX}) be an infra topological space. A set 'A' is called infra b-open if $A \subseteq iip(icp(A)) \cup icp(iip(A))$ and infra b- closed set if $iip(icp(A)) \cup icp(iip(A)) \subseteq A$.

Definition 3.5: Let (X, τ_{iX}) be an infra topological space. A set 'A' is called infra β -open if $A \subseteq icp(iip(icp(A)))$ and infra β - closed set if $iip(icp(iip(icp(A)))) \subseteq A$.

The collection of all classes of infra semi- open , infra pre- open , infra α -open , infra b-open , infra semi-preopen (or) infra β -open subsets of (X, τ_{iX}) are denoted by ISOP(A), IPOP(A), I α OP(A),IBOP(A), ISPOP(A) respectively.

For a subset A of a space (X, τ_{iX}) the infra b-closure (respectively infra semi-closure, infra pre-closure, infra semi pre-closure) of A, denoted by $bicp(A)$

(respectively $sicp(A), picp(A), spicp(A)$) is the intersection of all infra b -closed (respectively infra semi-closed, infra pre-closed, infra semi pre-closed) subsets of (X, τ_{ix}) containing A .

Dually, the infra b -interior (respectively infra semi-interior, infra pre-interior, infra semi-pre-interior) of A , denoted by $biip(A)$ (respectively $siip(A), piip(A), spiip(A)$) is the union of all infra b -open (respectively infra semi-open, infra pre-open, infra semi-pre-open) subsets of (X, τ_{ix}) contained in A .

Proposition 3.6: Let A be a subset of a space (X, τ_{ix}) . Then

- (1) $sicp(A) = A \cup (iip(icp(A)))$ and $siip(A) = A \cap (icp(iip(A)))$
- (2) $picp(A) = A \cup (icp(iip(A)))$ and $piip(A) = A \cap (iip(icp(A)))$
- (3) $spicp(A) = A \cup (iip(icp(iip(A))))$ and $spiip(A) = A \cap (icp(iip(icp(A))))$
- (4) $sicp(siip(A)) = siip(A) \cup (iip(icp(iip(A))))$
- (5) $picp(piip(A)) = piip(A) \cup (icp(iip(A)))$
- (6) $spicp(spiip(A)) = spiip(spicp(A))$

Theorem 3.7: In an infra topological space (X, τ_{ix})
 (i) Every infra semi-open set is infra b -open set. (ii) Every infra pre-open set is infra b -open set.

Proof: The result is Obvious.

The converse of the above theorem need not be true as shown by the following example.

Example 3.8: Let (X, τ_{ix}) be an infra topological space. Let $X = \{a, b, c\}$, $\tau_{ix} = \{\phi, X, \{b\}, \{c\}\}$. Here $\{b, c\}$ is infra b -open set but it is not infra semi-open set and $\{a, b\}$ is infra b -open set but it is not infra pre-open set.

Proposition 3.9: For a subset A of a space X the following are equivalent:

- a) A is infra b -open set.
- b) $A = piip(A) \cup siip(A)$
- c) $A \subseteq (picp(piip(A)))$

Proof: Let $A \subseteq X$, Where (X, τ_{ix}) is an infra topological space.

(a) \Rightarrow (b) Let A be infra b -open set.

(i.e) $A \subseteq iip(icp(A)) \cup icp(iip(A))$.

Then by proposition (3.6)

$$piip(A) \cup siip(A) = (A \cap iip(icp(A))) \cup (A \cap (icp(iip(A)))) = A \cap (iip(icp(A)) \cup (icp(iip(A)))) = A$$

Therefore $A = piip(A) \cup siip(A)$

(b) \Rightarrow (c), By Proposition (3.6) We have, $A = piip(A) \cup siip(A) = piip(A) \cup (A \cap icp(iip(A))) \subseteq piip(A) \cup (icp(iip(A))) = (picp(piip(A)))$

(c) \Rightarrow (a), By Proposition (3.6) We have $A \subseteq piip(A) \cup (icp(iip(A))) \subseteq iip(icp(A)) \cup (icp(iip(A)))$.

Therefore A is infra b -open set.

Theorem 3.10: Let A be a subset of a space (X, τ_{ix}) . Then

- (a) $bicp(A) = sicp(A) \cap picp(A)$
- (b) $biip(A) = siip(A) \cup piip(A)$

Proof: Obvious.

Theorem 3.11: If A be a subset of a space (X, τ_{ix}) , then $biip(bicp(A)) = bicp(biip(A))$.

Proof: Let A be a subset of a space (X, τ_{ix}) .

$$\text{Now } biip(bicp(A)) = siip(bicp(A)) \cup piip(bicp(A)) = bicp(siip(A)) \cup piip(bicp(A))$$

$$= sicp(siip(A)) \cup piip(picp(A)) \text{ ---- (1)}$$

$$\& bicp(biip(A)) = bicp(siip(A) \cup piip(A)) = bicp(siip(A)) \cup bicp(piip(A))$$

$$= sicp(siip(A)) \cup piip(picp(A)) \text{ ---- (2)}$$

Hence, From (1) & (2), $biip(bicp(A)) = bicp(biip(A))$. Hence the theorem.

Proposition 3.12: Let A be a infra b -open set such that $iip(A) = \phi$, then A is infra pre-open set.

Proof: The result is obvious.

Theorem 3.13: In an Infra topological space X , we have the following:

- (i) Every infra open set is infra α -open set.
- (ii) Every infra α -open set is both infra semi-open set and infra pre-open set.
- (iii) Every infra semi-open set and every pre-open set is infra β -open set.

The converse of the above theorem is not true as shown by the following example.

Example 3.14: Let $X = \{a, b, c\}$, $\tau_{ix} = \{\phi, X, \{a\}, \{b\}, \{c\}, \{a, b\}\}$. Here $\{b, c\}$ is infra α -open set but it is not infra open set.

Example 3.15: Let $X = \{a, b, c\}$, $\tau_{ix} = \{\phi, X, \{a\}, \{c\}\}$. Here $\{b, c\}$ is infra semi-open set but it is not infra α -open set. And here $\{a, c\}$ is infra pre-open set but it is not infra α -open set.

Example 3.16: Let $X = \{a, b, c\}$, $\tau_{ix} = \{\phi, X, \{a\}, \{c\}\}$. Here $\{a, c\}$ is infra β -open set but it is not infra semi-open set. And here $\{a, b\}$ is infra β -open set but it is not infra pre-open set.

Theorem 3.17: In an Infra topological space X , every infra b -open set (b -closed set) is an infra β -open set (β -closed set).

Proof: Let A be a infra b -open set in X Then $A \subseteq icp(iip(A)) \cup iip(icp(A)) \subseteq icp(iip(icp(A))) \cup iip(icp(A) \subseteq icp(iip(icp(A)))$.

Therefore A is infra β -open set.

The converse is not true as seen in the following example:

Example 3.18: Let $X = \{a, b, c\}$, $\tau_{ix} = \{\phi, X, \{b\}, \{c\}\}$. Here $\{a\}$ is infra β -open set but it is not infra b -open set.

Proposition 3.19 : (a) The intersection of an infra-open set and a infra b -open set is a infra b -open set.

(b)The finite union of any family of *infra b – open set* may fail to be a *infra b – open set*.

Proof: (a) The result is obvious. (b)In Example (3.5), both $\{a\}$ and $\{b\}$ are *infra b – open sets*, but their union $\{a, b\}$ is not a *b – open set* .

4. Infra B-Continuous Function In Infra Topological Space: In this section we introduce a new type of *infra continuous functions* and obtain some of their properties.

Definition 4.1: Let (X, τ_X) and (Y, τ_Y) be two topological spaces and τ_{iX} be an associated *infra topology* with τ_X .

A function $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ is called an *infra b^i -continuous function* if the inverse image of each *infra open set* in Y is an *infra b-open set* in (X, τ_{iX}) .

Definition 4.2:Let (X, τ_X) and (Y, τ_Y) be two topological spaces and τ_{iX} be an associated *infra topology* with τ_X .

A function $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ is called an *infra β - continuous function* (respectively *infra α - continuous, infra pre- continuous, infra semi-continuous*), if the inverse image of each *infra open set* in Y is an *infra β -open* (respectively *infra α -open, infra pre- open, infra semi- open*), set in (X, τ_{iX}) .

Theorem 4.3: Every *infra continuous function* is *infra b-continuous function*.

Proof:Let $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ be a *infra continuous function* and A is *infra open* in Y . Then $f^{-1}(A)$ is an *infra open set* in X . Since τ_{iX} is associated with τ_X , then $\tau_{iX} \subset \tau_X$. Therefore, $f^{-1}(A)$ is *infra open* in X and it is *infra b-open* in X . Hence f is *infra b-continuous*.

The converse of the above theorem is not true as shown in the following example.

Example 4.4: Let $X=\{a, b, c\}, \tau = \{\phi, X, \{a\}, \{b\}, \{a, b\}\}, \tau_{iX} = \{\phi, X, \{a\}, \{b\}\}$

A function $f: (X, \tau_X) \rightarrow (X, \tau_X)$ is an *identity function*. Here the inverse image of an *infra open set* $\{a, c\}$ is $\{a, c\}$ which not an *open set* in X is but it is *infra b-open set*. Then f is *infra b-continuous* but it is not *continuous*.

The following Example shows that *infra b-continuous function* need not be *infra semi-continuous function*.

Example 4.5: Let $X=\{a, b, c\}$ and $\tau_X = \{\phi, X, \{a\}, \{b\}, \{a, b\}, \{a, c\}\}, \tau_{iX} = \{\phi, X, \{a\}, \{b\}, \{a, c\}\}$. Suppose $Y= \{a, b\}$ with the topology $\tau_Y = \{\phi, X, \{a\}\}$. Define the function $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ by $f(a) =a, f(b) =a, f(c) =b$.

Here f is *infra b -continuous function* but not *infra semi-continuous function*.

The following Example shows that *infra α - continuous function* need not be *infra-continuous function*.

Example 4.6: Let $X=\{a, b, c\}$ and $\tau_X = \{\phi, X, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}\}, \tau_{iX} = \{\phi, X, \{a\}, \{b\}, \{c\}, \{a, b\}\}$. Suppose $Y= \{1, 2, 3\}$ with the topology $\tau_Y = \{\phi, X, \{1\}, \{2\}, \{1, 2\}\}$. Define the

function $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ by $f(a) =3, f(b) =1, f(c) =2$. Here f is *infra α -continuous function* but not *infra α -continuous function*.

The following Example shows that *infra pre-continuous function* need not be *infra α -continuous function*.

Example 4.7: Let $X=\{a, b, c\}$, and $\tau_X = \{\phi, X, \{b\}, \{c\}, \{a, c\}, \{b, c\}\}, \tau_{iX} = \{\phi, X, \{b\}, \{c\}, \{a, c\}\}$. Suppose $Y= \{1, 2, 3\}$ with the topology $\tau_Y = \{\phi, X, \{1\}, \{3\}, \{1, 3\}\}$. Define the function $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ by $f(a) =2, f(b) =1, f(c) =3$. Here f is *infra pre-continuous function* but not *infra α -continuous*.

The following Example shows that *infra semi-continuous function* need not be *infra α -continuous function*.

Example 4.8:Let $X=\{a, b, c\}$, and $\tau_X = \{\phi, X, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}\}, \tau_{iX} = \{\phi, X, \{a\}, \{b\}, \{c\}, \{a, c\}\}$. Suppose $Y= \{1, 2, 3\}$ with the topology $\tau_Y = \{\phi, X, \{1\}, \{2\}, \{1, 2\}, \{1, 3\}\}$. Define the function $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ by $f(a) =1, f(b) =3, f(c) =2$. Here f is *infra semi-continuous function* but not *infra α -continuous function*.

The following Example shows that *infra β -continuous function* need not be *infra b-continuous function*.

Example 4.9:Let $X=\{a, b, c\}$ and $\tau_X = \{\phi, X, \{b\}, \{c\}, \{a, c\}, \{b, c\}\}, \tau_{iX} = \{\phi, X, \{a\}, \{b\}, \{c\}\}$. Suppose $Y= \{1, 2, 3\}$ with the topology $\tau_Y = \{\phi, X, \{1\}, \{2\}, \{1, 2\}, \{1, 3\}\}$. Define the function $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ by $f(a) =1, f(b) =2, f(c) =3$. Here f is *infra β -continuous function* but not *infra b -continuous function*.

The following Example shows that *infra b-continuous function* need not be *infra pre-continuous function*.

Example 4.10:Let $X=\{a, b, c\}$ and $\tau_X = \{\phi, X, \{a\}, \{c\}, \{a, b\}, \{a, c\}\}, \tau_{iX} = \{\phi, X, \{a\}, \{c\}\}$. Suppose $Y= \{1, 2, 3\}$ with the topology $\tau_Y = \{\phi, X, \{1\}, \{2\}, \{1, 2\}, \{1, 3\}\}$. Define the function $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ by $f(a) =1, f(b) =3, f(c) =2$. Here f is *infra b-continuous function* but not *infra pre - continuous function*.

Theorem 4.11: Let $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ be a function from an *infra space* X to an *infra space* Y . Then the following statements are true:(i) f is *infra b –continuous*(ii)The inverse image of each *infra - closed set* in Y is *infra b-closed set* in X .

Proof: (i) \implies (ii) Let A be *infra-closed set* in Y . Then A^c is *infra-open set*. Then $f^{-1}(A^c) \in$ *infra b-open set* of $X \implies X - f^{-1}(A) \in$ *infra b-open set* of X . Hence $f^{-1}(A)$ is an *infra b-closed set* in X .

(ii) \implies (i) Let B be *infra-open set* in Y . Then B^c is *infra-closed set*. And by (ii) we have $f^{-1}(B^c) \in$ *infra b-closed set* of $X \implies X - f^{-1}(B) \in$ *infra b-closed set* in X . Hence $f^{-1}(B)$ is an *infra b-open set* in X . Therefore f is an *infra b-continuous function*.

Theorem 4.12: Let (X, τ_X) , (Y, τ_Y) , (Z, τ_Z) be three topological spaces. If a map $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ is an infra b-continuous map & $g: (Y, \tau_Y) \rightarrow (Z, \tau_Z)$ is a continuous map then $g \circ f: (X, \tau_X) \rightarrow (Z, \tau_Z)$ is an infra b-continuous.

Proof: Obvious

5. Infra B-Irresolute Function In Infra Topological Space: Definition 5.1:

Let (X, τ_X) and (Y, τ_Y) be represent two topological spaces. Let (X, τ_{iX}) and (Y, τ_{iY}) be two associated infra topological spaces. A function $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ is said to be infra b-irresolute function if the inverse image of each infra b-open set in τ_{iY} is an τ_{iX} -infra b-open set in X.

Theorem 5.2: A function $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ is infra b-irresolute function if and only if the inverse image of each infra b-closed set in τ_{iY} is an τ_{iX} -infra b-closed set in X.

Theorem 5.3: Every infra b-irresolute function is infra b-continuous function.

Proof: Let $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ is infra b-irresolute function. Let A be infra closed set in Y then A is infra b-closed set in Y. Since f is infra b-irresolute function,

$f^{-1}(A)$ is infra b-closed set in X. Hence f is infra b-continuous function.

Theorem 5.4: Let (X, τ_X) , (Y, τ_Y) , (Z, τ_Z) be three topological spaces. Let $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ & $g: (Y, \tau_Y) \rightarrow (Z, \tau_Z)$ be two functions. Then

(i) $g \circ f: (X, \tau_X) \rightarrow (Z, \tau_Z)$ is infra b-irresolute if f and g is infra b-irresolute functions.

(ii) $g \circ f: (X, \tau_X) \rightarrow (Z, \tau_Z)$ is infra b-continuous if f is infra b-irresolute function and g is infra b-continuous function.

Proof: (i) Let $g: (Y, \tau_Y) \rightarrow (Z, \tau_Z)$ is infra b-irresolute function and let O be infra b-closed of Z. Since g is infra b-irresolute by definition of infra b-irresolute, $g^{-1}(O)$ is infra b-closed set in Y. Also $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ is infra b-irresolute, so $f^{-1}(g^{-1}(O)) = (g \circ f)^{-1}(O)$ is infra b-closed. Thus $g \circ f: (X, \tau_X) \rightarrow (Z, \tau_Z)$ is infra b-irresolute. (ii) Let O be infra b-closed set of Z. Since $g: (Y, \tau_Y) \rightarrow (Z, \tau_Z)$ is infra b-continuous function, $g^{-1}(O)$ is infra b-closed set in Y. Also $f: (X, \tau_X) \rightarrow (Y, \tau_Y)$ is infra b-irresolute, so every infra b-closed set of Y is infra b-closed in X. Therefore $f^{-1}(g^{-1}(O)) = (g \circ f)^{-1}(O)$ is infra b-closed of X. Thus $g \circ f: (X, \tau_X) \rightarrow (Z, \tau_Z)$ is infra b-continuous.

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