

$rg^{}b^\mu$ -LOCALLY CLOSED SETS AND $rg^{**}b^\mu$ -LOCALLY CONTINUOUS FUNCTIONS IN SUPRA TOPOLOGICAL SPACES**

K.LUDI JANCY JENIFER, K.INDIRANI

Abstract: The aim of this paper is to introduce and investigate a new decomposition of sets namely supra $rg^{**}b$ - locally closed sets and a new decomposition of continuous maps called supra $rg^{**}b$ -locally continuous functions. This paper also discusses some of their properties and characteristics.

Keywords: supra $rg^{**}b$ -LC sets($rg^{**}b^\mu$ -LC), supra $rg^{**}b$ -LC* sets($rg^{**}b^\mu$ -LC*), supra $rg^{**}b$ -LC** sets($rg^{**}b^\mu$ -LC**), $rg^{**}b^\mu$ -LC-continuous, $rg^{**}b^\mu$ -LC-irresolute.

1.Introduction:Palaniappan and Rao[11] defined a set called regular generalized closed set.Ganster and Reily[5] introduced and studied different notions of generalized continuity and gave a decomposition of sets and continuity. Arockiarani et al[1] introduced regular generalized locally closed sets and investigated the classes of regular generalized locally continuous functions in topological spaces.The notion of supra topological spaces was introduced by Mashhour et al[10] in 1983.Ravi et al[12] introduced supra rg-closed set. Dayana Mary and Nagaveni[2,3] introduced supra g-locally closed sets and supra rg-locally closed sets and studied their basic properties.In 2015,Jeyanthi and Janaki[6],introduced πg^R -Locally closed sets in supra topological spaces.In the year 2012,Krishnaveni and Vigneshwaran[8], introduced bT-locally closed sets and bT-locally continuous functions in supra topological spaces.In 2016,Ludi jancyjenifer and Indirani[9] introduced a new class of set called $rg^{**}b^\mu$ closed set in supra topological space.

In this paper, we introduce the concept of $rg^{**}b^\mu$ locally closed sets and study its basic properties. Further, the concept of $rg^{**}b^\mu$ -LC continuous function and $rg^{**}b^\mu$ -LC irresolute function are introduced and studied.

2.Preliminaries: Throughout this paper (X,τ) and (X,μ) represent the topological space and supra topological space respectively on which no separation axioms are assumed , unless explicitly stated.

Definition 2.1[10]: Let X be a non-empty set. The subfamily $\mu \subset P(X)$ is said to be a supra topology on X if $X \in \mu$ and $\emptyset \in \mu$ and μ is closed under arbitrary unions. The pair (X,μ) is called a supra topological space. The elements of μ are said to be supra open in (X,μ) and its complement is supra closed set. We call μ as supra topology associated with τ if $\tau \subset \mu$.

Definition 2.2[10]:Let A be a subset of (X, μ) . Then
 (i) The **supra closure** of a set A is denoted by $cl^\mu(A)$ defined as $cl^\mu(A) = \bigcap \{B: B \text{ is supra closed and } A \subset B\}$
 (ii) The **supra interior** of a set A is denoted by $int^\mu(A)$ defined as $int^\mu(A) = \bigcup \{ B: B \text{ is supra open and } B \subset A\}$

Definition 2.3[2,3]:Let A and B be subsets of X. Then A and B are said to be supra separated, if $A \cap cl^\mu(B) = \emptyset$ and $cl^\mu(A) \cap B = \emptyset$.

Definition 2.4: Let (X, μ) be a supra topological space.

A subset A of X is called

(i) **supra regular generalized star star b-closed set**[9](briefly $rg^{**}b^\mu$ -closed set) if $rg^{**}bcl^\mu(A) \subseteq U$ whenever $A \subseteq U$ and U is supra open in X.

(ii) **supra regular open**[5] if $A = int^\mu(cl^\mu(A))$ and **supra regular closed** if $A = cl^\mu(int^\mu(A))$.

Definition 2.5: Let (X, τ) and (Y, σ) be two topological spaces and $\tau \subset \mu, \sigma \subset \lambda$. A map $f: (X, \mu) \rightarrow (Y, \lambda)$ is called

supra continuous[2] if $f^{-1}(V)$ is a supra closed of (X, μ_1) for every supra closed set V of (Y, μ_2) .

supra regular- continuous[4] if $f^{-1}(V)$ is a supra -regular closed of (X, μ_1) for every supra closed set V of (Y, μ_2) .

$rg^{}b^\mu$ -continuous**[9] if $f^{-1}(V)$ is $rg^{**}b^\mu$ -closed set of (X, μ) for every closed set V of (Y, σ) .

(i) **$rg^{**}b^\mu$ -irresolute**[9] if $f^{-1}(V)$ is $rg^{**}b^\mu$ -closed in X for every $rg^{**}b^\mu$ -closed set V of Y.

supra R-map[5] (**R^μ - map**) if $f^{-1}(V)$ is supra regular closed in X for every supra regular closed in Y.

Definition 2.6:A space X is said to be **$rg^{**}b^\mu$ - $T_{1/2}$** space if every $rg^{**}b^\mu$ -closed set is R^μ -closed.

Definition 2.7: A subset S of a supra topological space X

1. **supra locally closed**[7,12](briefly LC^μ -closed set) if $S = A \cap B$, where A is supra open and B is supra closed in X.

2. **supra regular locally closed**[3](briefly R^μ -LC) if $S = A \cap B$, where A is supra regular open and B is supra regular closed in X.

Definition 2.8: Let (X,τ) and (Y,σ) be two topological spaces , $\tau \subset \mu, \sigma \subset \lambda$. A map $f: (X,\mu) \rightarrow (Y,\lambda)$ is called

(i) **supra LC continuous**[2] if the $f^{-1}(V)$ is supra locally closed in X for every supra closed set V in Y.

(ii) **R^μ -LC continuous** [4] if $f^{-1}(V)$ is R^μ -LC in X for every supra closed set V in Y.

(iii) R^μ -LC irresolute[5](R^μ -LC map) if $f^1(V)$ is R^μ -LC in X for every R^μ -LC set V in Y .

3. $rg^{}b^\mu$ -locally closed sets**

Definition 3.1: A subset S of a supra topological space X is called

(i) $rg^{**}b^\mu$ -LC set if $S = A \cap B$, where A is $rg^{**}b^\mu$ -open in X and B is $rg^{**}b^\mu$ -closed in X .

(ii) $rg^{**}b^\mu$ -LC*-closed if $S = A \cap B$, where A is $rg^{**}b^\mu$ -open in X and B is supra closed in X .

(iii) $rg^{**}b^\mu$ -LC** closed if $S = A \cap B$, where A is supra open in X and B is $rg^{**}b^\mu$ -closed in X .

The collection of all $rg^{**}b^\mu$ -LC sets, $rg^{**}b^\mu$ -LC* and $rg^{**}b^\mu$ -LC** sets of X will be denoted by $rg^{**}b^\mu$ -LC(X), $rg^{**}b^\mu$ -LC*(X), $rg^{**}b^\mu$ -LC**(X).

Proposition 3.2: Every $rg^{**}b^\mu$ -closed set is $rg^{**}b^\mu$ -LC set and every $rg^{**}b^\mu$ -open set is $rg^{**}b^\mu$ -LC set.

Proof: Follows from the definition.

Theorem 3.3: Let A be a subset of (X, μ) . If A is supra locally regular closed, then $A \in rg^{**}b^\mu$ -LC*(X, μ) and $A \in rg^{**}b^\mu$ -LC**(X, μ) but not conversely.

Proof: obvious.

Example 3.4: Let $X = \{a, b, c\}, \mu = \{X, \emptyset, \{a, b\}, \{b, c\}\}$. Here the subset $\{c\} \in rg^{**}b^\mu$ -LC*(X, μ) and $rg^{**}b^\mu$ -LC**(X, μ) but $\{c\} \notin R^\mu$ -LC set.

Theorem 3.5: Let A be a subset of (X, μ) . If $A \in rg^{**}b^\mu$ -LC*(X, μ) (or) $rg^{**}b^\mu$ -LC**(X, μ) then A is $rg^{**}b^\mu$ -LC(X, μ) but not conversely.

Proof: Given $A \in rg^{**}b^\mu$ -LC*(X, μ) (or) $rg^{**}b^\mu$ -LC**(X, μ), by definition $A = U \cap V$, where U is $rg^{**}b^\mu$ -open set and V is supra closed set (or) U is supra open set and V is $rg^{**}b^\mu$ -closed set. Every supra closed set is $rg^{**}b^\mu$ -closed set, therefore V is $rg^{**}b^\mu$ -closed set (or) every supra open set is $rg^{**}b^\mu$ -open set, therefore U is $rg^{**}b^\mu$ -open set. Then A is $rg^{**}b^\mu$ -LC(X, μ).

Example 3.6: Let $X = \{a, b, c\}$ and $\mu = \{X, \phi, \{a, b\}, \{a, c\}\}$. In this $(X, \mu), \{b, c\} \in rg^{**}b^\mu$ -LC(X, μ) but $\{b, c\} \notin rg^{**}b^\mu$ -LC*(X, μ) and $rg^{**}b^\mu$ -LC**(X, μ).

Theorem 3.7: Let A be a subset of (X, μ) . If $A \in S$ -LC(X, μ) then A is $rg^{**}b^\mu$ -LC(X, μ) but not conversely.

Proof: Given $A \in S$ -LC, by definition $A = U \cap V$, where U is supra open set and V is supra closed set. Since every supra open set is $rg^{**}b^\mu$ -open set and every supra closed set is $rg^{**}b^\mu$ -closed set. Then $A \in rg^{**}b^\mu$ -LC(X, μ).

Example 3.8: Let $X = \{a, b, c, d\}$ and $\mu = \{X, \phi, \{b\}, \{c\}, \{b, c\}, \{c, d\}, \{b, d\}, \{b, c, d\}\}$. In this $(X, \mu), \{b, c\} \in rg^{**}b^\mu$ -LC(X, μ) but $\{b, c\} \notin S$ -LC(X, μ).

Remark 3.9: The union of two $rg^{**}b^\mu$ -LC*(X, μ) sets need not be $rg^{**}b^\mu$ -LC*(X, μ).

Example 3.10: In example 3.4, let $A = \{a\}$ and $B = \{c\}$. Then A and B belongs to $rg^{**}b^\mu$ -LC*(X, μ), but their union $\{a, c\} \notin rg^{**}b^\mu$ -LC*(X, μ).

Theorem 3.11: For a subset A of X , the following are equivalent.

(i) $A \in rg^{**}b^\mu$ -LC*(X, μ).

(ii) $A = U \cap cl^\mu(A)$ for some supra $rg^{**}b^\mu$ -open set U .

Proof: (i) \Rightarrow (ii): Let $A \in rg^{**}b^\mu$ -LC*(X, μ). Then there exists a $rg^{**}b^\mu$ -open set U and a supra closed set V such that $A = U \cap V$. Since $A \subset U$ and $A \subset cl^\mu(A)$, $A \subset U \cap cl^\mu(A)$.

Let $A = U \cap V$ and $A \subset V$, $cl^\mu(A) \subset cl^\mu(V) = V$, since V is supra closed.

Now, $A = U \cap V \supset U \cap cl^\mu(A)$ implies $A \supset U \cap cl^\mu(A)$ and hence $A = U \cap cl^\mu(A)$.

(ii) \Rightarrow (i): Let $A = U \cap cl^\mu(A)$ for some $rg^{**}b^\mu$ -open set U . clearly $cl^\mu(A)$ is supra closed and hence $A \in rg^{**}b^\mu$ -LC*(X, μ).

Theorem 3.12: Let A be a subset of X and if $A \in rg^{**}b^\mu$ -LC(X, μ), then $A = U \cap rg^{**}b^\mu$ -cl(A) for some $rg^{**}b^\mu$ -open set U .

Proof: Let $A \in rg^{**}b^\mu$ -LC(X, μ). Then there exists a $rg^{**}b^\mu$ -open subset U and a $rg^{**}b^\mu$ -closed subset V such that $A = U \cap V$. Since $A \subset U$ and $A \subset rg^{**}b^\mu$ -cl(A), $A \subset U \cap rg^{**}b^\mu$ -cl(A).

Since $A = U \cap V$ and V is $rg^{**}b^\mu$ -closed, $rg^{**}b^\mu$ -cl(V) = V . Also, since $A \subset V$, $rg^{**}b^\mu$ -cl(A) $\subset rg^{**}b^\mu$ -cl(V) = V . Therefore $rg^{**}b^\mu$ -cl(A) $\subset V$. Now, let $A = U \cap V$, $A \supset U \cap rg^{**}b^\mu$ -cl(A) and hence $A = U \cap rg^{**}b^\mu$ -cl(A).

Proposition 3.13: Let X be a $rg^{**}b^\mu$ - $T_{1/2}$ -space. Then $rg^{**}b^\mu$ -LC(X, μ) = R^μ -LC(X, μ)

Proof: Let $A \in rg^{**}b^\mu$ -LC(X, μ). Then there exists $rg^{**}b^\mu$ -open set U and $rg^{**}b^\mu$ -closed set V such that $A = U \cap V$. Since X is a $rg^{**}b^\mu$ - $T_{1/2}$ -space, then U and V are supra regular open and supra regular closed respectively and hence $A \in R^\mu$ -LC(X, μ). The above implies $rg^{**}b^\mu$ -LC(X, μ) $\subset R^\mu$ -LC(X, μ).

On the other hand, let $A \in R^\mu$ -LC(X, μ). Then $A = U \cap V$, where U is R^μ -open and V is R^μ -closed. But every R^μ -closed set is $rg^{**}b^\mu$ -closed. Hence U is $rg^{**}b^\mu$ -open and V is $rg^{**}b^\mu$ -closed. The above implies R^μ -LC(X, μ) $\subset rg^{**}b^\mu$ -LC(X, μ). Hence $rg^{**}b^\mu$ -LC(X, μ) = R^μ -LC(X, μ).

Proposition 3.14: If X is a supra $rg^{**}b^\mu$ - $T_{1/2}$ -space, then $rg^{**}b^\mu$ -LC(X, μ) $\subset LC^\mu(X, \mu)$.

Proof: Let $A \in rg^{**}b^\mu$ -LC(X, μ). Then there exists $rg^{**}b^\mu$ -open set U and $rg^{**}b^\mu$ -closed set V such that $A = U \cap V$. Since X is a $rg^{**}b^\mu$ - $T_{1/2}$ -space, then U and V are R^μ -open and R^μ -closed respectively. Then U is supra open and V is supra closed. The above implies A is supra locally closed in X . Hence $rg^{**}b^\mu$ -LC(X, μ) $\subset LC^\mu(X, \mu)$.

Proposition 3.15: If X is a $rg^{**}b^\mu$ - $T_{1/2}$ -space, then $rg^{**}b^\mu$ -LC(X, μ) $\subset rg^{**}b^\mu$ -LC*(X, μ) and $rg^{**}b^\mu$ -LC(X, μ) $\subset rg^{**}b^\mu$ -LC**(X, μ).

Proof: Let $A \in rg^{**}b^\mu$ -LC(X, μ). Then there exists $rg^{**}b^\mu$ -open set U and $rg^{**}b^\mu$ -closed set V such that $A = U \cap V$. Since X is $rg^{**}b^\mu$ - $T_{1/2}$ -space, V is R^μ -closed and hence $A \in rg^{**}b^\mu$ -LC*(X, μ). Hence

$rg^{**}b^\mu$ -LC(X,μ) $\subset rg^{**}b^\mu$ -LC*(X,μ). Similarly, we prove $rg^{**}b^\mu$ -LC(X,μ) $\subset rg^{**}b^\mu$ -LC**(X,μ).

Theorem 3.16: For a subset A of X, if $A \in rg^{**}b^\mu$ -LC**(X,μ), then there exists a supra open set U such that $A=U \cap rg^{**}b^\mu$ -cl(A).

Proof: Let $A \in rg^{**}b^\mu$ -LC**(X,μ), then there exists a supra open set U and $arg^{**}b^\mu$ -closed set V such that $A=U \cap V$. Since $A \subset U$ and $A \subset rg^{**}b^\mu$ -cl(A), $A \subset U \cap rg^{**}b^\mu$ -cl(A). Now $A \subset V$, $rg^{**}b^\mu$ -cl(A) $\subset rg^{**}b^\mu$ -cl(V)=V, as V is $arg^{**}b^\mu$ -closed. $U \cap rg^{**}b^\mu$ -cl(A) $\subset U \cap V = A$. Thus $U \cap rg^{**}b^\mu$ -cl(A) $\subset A$ and hence $A = U \cap rg^{**}b^\mu$ -cl(A).

4. $rg^{}b^\mu$ -locally continuous functions**

Definition 4.1: Let (X,τ) and (Y,σ) be two topological spaces and $\tau \subseteq \mu$ and $\sigma \subseteq \lambda$. A function $f: (X,\mu) \rightarrow (Y,\lambda)$ is

- (i) $rg^{**}b^\mu$ -LC continuous if $f^{-1}(A) \in rg^{**}b^\mu$ -LC(X,μ) for each $A \in (Y,\lambda)$.
- (ii) $rg^{**}b^\mu$ -LC* continuous if $f^{-1}(A) \in rg^{**}b^\mu$ -LC*(X,μ) for each $A \in (Y,\lambda)$.
- (iii) $rg^{**}b^\mu$ -LC** continuous if $f^{-1}(A) \in rg^{**}b^\mu$ -LC**(X,μ) for each $A \in (Y,\lambda)$.

Definition 4.2: Let (X,τ) and (Y,σ) be two topological spaces and μ and λ be supra topologies associated with τ and σ respectively. A function $f: (X,\mu) \rightarrow (Y,\lambda)$ is

- (i) $rg^{**}b^\mu$ -LC irresolute if $f^{-1}(A) \in rg^{**}b^\mu$ -LC(X,μ) for each $A \in rg^{**}b^\mu$ -LC(Y,λ).
- (ii) $rg^{**}b^\mu$ -LC* irresolute if $f^{-1}(A) \in rg^{**}b^\mu$ -LC*(X,μ) for each $A \in rg^{**}b^\mu$ -LC*(Y,λ).
- (iii) $rg^{**}b^\mu$ -LC** irresolute if $f^{-1}(A) \in rg^{**}b^\mu$ -LC**(X,μ) for each $A \in rg^{**}b^\mu$ -LC**(Y,λ).

Theorem 4.3: Every R^μ -LC continuous function is $rg^{**}b^\mu$ -LC continuous.

Proof: Obvious.

Remark 4.4: Converse of the above need not be true as shown in the following example.

Example 4.5: Let $X=\{a,b,c,d\}=Y$, $\mu=\{X,\emptyset, \{b\},\{c\},\{b,c\},\{c,d\},\{b,d\},\{b,c,d\}\}$, $\lambda=\{Y,\emptyset, \{b\},\{c\},\{a,b\},\{b,c\},\{a,c\},\{a,b,c\}\}$. Let $(X,\mu) \rightarrow (Y,\lambda)$ be an identity map. Here the inverse image of supra closed sets in Y are not R^μ -LC in X but $rg^{**}b^\mu$ -LC in X. Hence $rg^{**}b^\mu$ -LC continuous function need not be R^μ -LC continuous.

Theorem 4.6: If $f: (X,\mu) \rightarrow (Y,\lambda)$ is $rg^{**}b^\mu$ -LC continuous and X is $rg^{**}b^\mu$ - $T_{1/2}$ -space, then f is LC continuous

Proof: Let V be a supra open set of Y. Since f is $rg^{**}b^\mu$ -LC continuous, $f^{-1}(V)$ is $rg^{**}b^\mu$ -LC in X. Since X is a $rg^{**}b^\mu$ - $T_{1/2}$ -space, every $rg^{**}b^\mu$ -closed set ($rg^{**}b^\mu$ -open set) in X is R^μ -closed (R^μ -open) in X and hence supra closed (supra open) in X. Then $f^{-1}(V)$ is supra locally closed in Y and hence f is LC continuous.

We have the following theorem concerning the composition of functions.

Theorem 4.7: If $f: (X,\mu) \rightarrow (Y,\lambda)$ and $g: (Y,\lambda) \rightarrow (Z,\xi)$ be two functions. Then

- a) $g \circ f$ is $rg^{**}b^\mu$ -LC irresolute if f and g are $rg^{**}b^\mu$ -LC irresolute.
- b) $g \circ f$ is $rg^{**}b^\mu$ -LC* irresolute if f and g are $rg^{**}b^\mu$ -LC* irresolute.
- c) $g \circ f$ is $rg^{**}b^\mu$ -LC** irresolute if f and g are $rg^{**}b^\mu$ -LC** irresolute.
- d) $g \circ f$ is $rg^{**}b^\mu$ -LC* continuous if f is $rg^{**}b^\mu$ -LC* continuous and g is supra continuous.
- e) $g \circ f$ is $rg^{**}b^\mu$ -LC continuous if f is $rg^{**}b^\mu$ -LC continuous and g is supra continuous.
- f) $g \circ f$ is $rg^{**}b^\mu$ -LC* continuous if f is $rg^{**}b^\mu$ -LC* irresolute and g is $rg^{**}b^\mu$ -LC* continuous.
- g) $g \circ f$ is $rg^{**}b^\mu$ -LC** continuous if f is $rg^{**}b^\mu$ -LC** irresolute and g is $rg^{**}b^\mu$ -LC** continuous.
- h) $g \circ f$ is $rg^{**}b^\mu$ -LC continuous if f is $rg^{**}b^\mu$ -LC irresolute and g is $rg^{**}b^\mu$ -LC continuous.

Proof: Obvious.

Theorem 4.8: Let (X,τ) and (Y,σ) be two topological spaces and μ and λ be a supra topology associated with τ and σ . Let $f: (X,\tau) \rightarrow (Y,\sigma)$ be a function. If f is $rg^{**}b^\mu$ -LC* continuous (or) $rg^{**}b^\mu$ -LC** continuous, then it is $rg^{**}b^\mu$ -LC-continuous.

Proof: Let $f: (X,\tau) \rightarrow (Y,\sigma)$ be a function. If f is $rg^{**}b^\mu$ -LC* continuous (or) $rg^{**}b^\mu$ -LC** continuous, by definition $f^{-1}(A) \in rg^{**}b^\mu$ -LC*(X,μ), and $f^{-1}(A) \in rg^{**}b^\mu$ -LC**(X,μ) for each $A \in \sigma$. $f^{-1}(A) \in rg^{**}b^\mu$ -LC(X,μ). Then it is $rg^{**}b^\mu$ -LC-continuous.

Theorem 4.9: Let (X,τ) and (Y,σ) be two topological spaces and μ and λ be a supra topologies associated with τ and σ respectively. Let $f: (X,\tau) \rightarrow (Y,\sigma)$ be a function. If f is $rg^{**}b^\mu$ -LC-irresolute (resp., $rg^{**}b^\mu$ -LC*-irresolute, and $rg^{**}b^\mu$ -LC**-irresolute), then it is $rg^{**}b^\mu$ -LC-continuous (resp., $rg^{**}b^\mu$ -LC*-continuous, and $rg^{**}b^\mu$ -LC**-continuous).

Proof: Let $f: (X,\tau) \rightarrow (Y,\sigma)$ be a function. Let A is supra closed of Y. By theorem, every supra closed set is $rg^{**}b^\mu$ -closed set, therefore A is $rg^{**}b^\mu$ -closed set. Since f is $rg^{**}b^\mu$ -LC-irresolute (resp., $rg^{**}b^\mu$ -LC*-irresolute, and $rg^{**}b^\mu$ -LC**-irresolute), $f^{-1}(A)$ is $rg^{**}b^\mu$ -LC set. Therefore f is $rg^{**}b^\mu$ -LC-continuous (resp., $rg^{**}b^\mu$ -LC*-continuous, and $rg^{**}b^\mu$ -LC**-continuous).

Theorem 4.10: If $f: (X,\mu) \rightarrow (Y,\lambda)$ is supra locally irresolute and $g: (Y,\lambda) \rightarrow (Z,\xi)$ is $rg^{**}b^\mu$ -LC-continuous and Y is $rg^{**}b^\mu$ - $T_{1/2}$ -space, then their composition $(g \circ f): (X,\mu) \rightarrow (Z,\xi)$ is supra locally continuous.

Proof: Let V be a supra closed set of Z. Since g is $rg^{**}b^\mu$ -LC-continuous, $g^{-1}(V)$ is $rg^{**}b^\mu$ -LC in Y. Since Y is $rg^{**}b^\mu$ - $T_{1/2}$ -space, $g^{-1}(V)$ is supra locally regular closed in Y and hence supra locally closed in Y. Since f is supra locally irresolute, then $f^{-1}(g^{-1}(V))$ is supra locally closed in X. Therefore, $(g \circ f)^{-1}(V)$ is

supra locally closed in X and hence $g \circ f$ is supra locally continuous.

Theorem 4.11: If $f: (X, \mu) \rightarrow (Y, \lambda)$ is $rg^{**}b^\mu$ -LC continuous and $g: (Y, \lambda) \rightarrow (Z, \xi)$ is $rg^{**}b^\mu$ -LC irresolute and Y is $rg^{**}b^\mu$ - $T_{1/2}$ -space, then their composition $(g \circ f): (X, \mu) \rightarrow (Z, \xi)$ is $rg^{**}b^\mu$ -LC irresolute.

Proof: Let V be a $rg^{**}b^\mu$ -LC set of Z . Since g is $rg^{**}b^\mu$ -L-irresolute, $g^{-1}(V)$ is $rg^{**}b^\mu$ -LC in Y . Since Y is $rg^{**}b^\mu$ - $T_{1/2}$ -space, $g^{-1}(V)$ is supra locally regular closed in Y and hence supra locally closed in Y . Since f is $rg^{**}b^\mu$ -LC continuous, $f^{-1}(g^{-1}(V))$ is $rg^{**}b^\mu$ -LC in X . Therefore, $(g \circ f)^{-1}(V)$ is $rg^{**}b^\mu$ -LC in X and hence $g \circ f$ is $rg^{**}b^\mu$ -LC irresolute.

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K. Ludijancyjenifer M. Phil scholar/ 54/11,Kamaraj road, opposite to Nirmala College, sungam,Coimbatore-18 / Bharathiyar University
K. Indirani, Associate Professor,S-3,D-Block,PGP village, Singanallur, Coimbatore-641005,Bharathiyar University .